REGULAR ARTICLE

# **Lithium–silicon Si**<sub>n</sub>**Li** ( $n = 2-10$ ) clusters and their anions: **structures, thermochemistry, and electron affinities**

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**Abstract** The molecular structures, electron affinities, and dissociation energies of neutral  $\sin L i (n = 2{\text -}10)$  species and their anions have been studied by the B3LYP and the BPW91 methods in conjunction with a DZP++ basis set. The geometries have been fully optimized with each of the proposed methods. The ground state structure of neutral Si*n*Li keeps the corresponding  $Si<sub>n</sub>$  framework unchanged. For anion, the corresponding  $\mathrm{Si}_n$  (or  $\mathrm{Si}_n^-$ ) framework changes largely when  $n \geq 7$ . To evaluate the stability of the resulting anions we have calculated the adiabatic electron affinity  $(EA_{ad})$ , the vertical electron affinity (EA<sub>vert</sub>), and the vertical detachment energy (VDE). The dissociating energies of Li from the lowest energy structures of neutral  $Si<sub>n</sub>Li$  and their anions are calculated to examine relative stabilities.

**Keywords**  $Si<sub>n</sub>Li$  · Electron affinities · Thermochemistry · DFT

# **1 Introduction**

Metal-silicon clusters have attracted much attention in the past decade. This has been attributed to their intrinsic interest

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from the point of view of chemical structure and bonding as well as their applications in modern industry  $[1-5]$  $[1-5]$ . Specially, alkali metal silicon clusters possess scientific value because it has been known that they serve as promoters in catalysts and can be used as power source material for spaceflight aero-crafts, emitters, and many other products.

Extensive experimental and theoretical studies on alkali metal-silicon clusters have recently been reported in the literature. For example, Kaya and co-workers [\[6](#page-7-2)[–8](#page-7-3)] have experimentally and theoretically explored the ionization potentials and electron affinities of sodium-doped silicon clusters. Zubarev et al. [\[9\]](#page-7-4) had recently published the electron affinity of  $Si<sub>6</sub>Na$  by means of photoelectron spectroscopy. In our group  $[10]$  we have investigated the neutral  $Si<sub>n</sub>Na$  $(n \leq 10)$  clusters and their anions by means of various density functional theory (DFT) schemes. For lithium-doped silicon clusters, Wang et al.  $[11]$  have explored the structures of  $Si<sub>n</sub>Li$  ( $n = 2-7$ ) clusters with the QCISD/6-311+G(d,p)// MP2/6-31G(d) method. Rabilloud and coworkers [\[12](#page-7-7)[–14\]](#page-7-8) reported the equilibrium geometries and electronic properties of neutral and charged  $\text{Si}_n\text{Li}_p^{(+)}$   $(n \leq p \leq 2)$  species by means of MP2 and DFT methodologies. These theoretical studies primarily focus on  $Si<sub>n</sub>Li$  clusters with small sizes  $(n \leq 7)$  and report their equilibrium geometries and ionization potentials.

Li et al. [\[15](#page-7-9)] had explored the structures of semiconductoralkali anions  $E_nA^-$  (A = K, Na, and Li; E = Ge, Si; and  $n = 1-10$  by means of MP2 method and predicted their vertical electron detachment energies using OVGF procedure. They suggested that the geometries of the ground state of Si*n*Li− and Si*n*Na− were identical to Si*n*K−. In fact, the geometries of  $Si<sub>n</sub>A$  and their anions are uncertainly similar to each other. For example, the geometries of Si9A<sup>−</sup> [\[10\]](#page-7-5) are not similar to each other. The geometries of Si<sub>3</sub>A are identical. On the other hand, several isomers of Si*n*K− reported by

Li [\[15](#page-7-9)] are not the lowest energy structures. All these facts spurred us to investigate  $Si<sub>n</sub>Li$  and their anions.

When predicting molecular energies, structures, and electron affinities, there are many theoretical approaches, but considering both reliability and computational expense, gradient corrected density functional theory has been shown to be effective for predicting electron affinities of many inorganic species such as the  $SiH_n/SiH_n^-$ ,  $Si_2H_n/Si_2H_n^-$ ,  $GeF_n/$ GeF<sub>n</sub><sup>-</sup>, SeF<sub>n</sub>/SeF<sub>n</sub><sup>-</sup>, and AsF<sub>n</sub>/AsF<sub>n</sub><sup>-</sup> systems [\[16](#page-7-10)[–19](#page-7-11)]. In this report we will focus on neutral Si*n*Li and their anions Si*n*Li− with *n* up to 10 atoms of Si in the gas phase. The methods used in this study are the carefully calibrated B3LYP and BPW91 theoretical approaches with a DZP++ basis sets. The objective of this research involves the (a) the predictions of the ground state structures of neutral  $Si<sub>n</sub>Li$  ( $n \leq 10$ ) and their anions; (b) the predictions of electron affinities of  $Si<sub>n</sub>Li$ ; (c) the evaluation of other properties including dissociation energies; and (d) to continue the previous work on silicon clusters [\[10](#page-7-5),[20,](#page-7-12)[21\]](#page-7-13).

#### **2 Computational methodology**

The two different density functional forms used here are (a) Becke's three-parameter hybrid exchange functional [\[22\]](#page-7-14) with the correlation functional of Lee et al. [\[23](#page-7-15)] (B3LYP) and (b) Becke's 1988 exchange functional [\[24](#page-7-16)] with the correlation functional of Perdew and Wang [\[25](#page-7-17)] (BPW91).

We have selected the B3LYP method because it has been calibrated by Schaefer and coworkers [\[26](#page-7-18)]. They also suggested that the BPW91 method might outperform the B3LYP scheme. Alternatively, for  $Si_n$ ,  $Si_nH$ , and  $Si_nNa$  clusters, the BPW91 scheme predicted the most reliable electron affinities [\[10](#page-7-5),[20,](#page-7-12)[21\]](#page-7-13). Hence, both the B3LYP and the BPW91 schemes were implemented throughout this study. The GAUSSIAN03 suite of codes was applied for the computations [\[27](#page-7-19)].

A standard double-ζ plus polarization (DZP) basis set with additional diffuse functions was utilized in this work. The DZ part of the basis set was constructed from the Huzinaga [\[28](#page-7-20)[–30](#page-7-21)], Dunning and Hay [\[31](#page-7-22)] set of contracted double-ζ Gaussian functions. The DZP basis set was then formed by the addition of a set of d-type polarization functions for Si and a set of p-type polarization functions for Li  $[\alpha_d(Si) = 0.5000, \alpha_p(Li) = 0.0205]$ . The DZP basis was augmented with diffuse functions; each atom received one additional s-type and one additional p-type functions. The diffuse function orbital exponents were determined in an "even-tempered sense" as a mathematical extension of the primitive set, according to the formula of Lee and Schae-fer [\[32](#page-7-23)]  $[\alpha_s(\text{Si}) = 0.02729, \alpha_p(\text{Si}) = 0.02500, \alpha_s(\text{Li}) =$ 0.00717523,  $\alpha_p(Li) = 0.00713759$ . The final contraction scheme for this basis set is Si (13s9p1d/7s5p1d) and Li (10s6p/5s4p). All Si*n*Li and Si*n*Li<sup>−</sup> (*n* = 2–10) stationary

point geometries were interrogated by the evaluation of their harmonic vibrational frequencies at the two different levels of theory.

The electron affinities are evaluated as the difference of total energies in the following manner: the adiabatic electron affinity is determined as  $EA_{ad} = E$  (zero-point corrected neutral)  $- E$  (zero-point corrected anion), the vertical electron affinity by EAvert = E (optimized neutral)  $- E$  (anion at optimized neutral geometry), and the vertical detachment energy of the anion by  $VDE = E$  (neutral at optimized anion  $geometry) - E$  (optimized anion).

### **3 Results and discussion**

# 3.1 Si<sub>2</sub>Li and Si<sub>2</sub>Li<sup>-</sup>

The geometries for the neutral  $Si<sub>2</sub>Li$  and its anion are displayed in Fig. [1.](#page-1-0) The geometrical parameters shown in Figs. [1,](#page-1-0) [2,](#page-2-0) [3,](#page-2-1) [4,](#page-2-2) [5,](#page-2-3) [6,](#page-2-4) [7,](#page-2-5) [8,](#page-3-0) and [9](#page-3-1) are calculated at the B3LYP level with the remainder of the parameters displayed in the supporting information. For neutral  $Si<sub>2</sub>Li$ , Wang et al. [\[11](#page-7-6)], and Sporea et al. [\[12](#page-7-7),[14\]](#page-7-8) have reported that the geometries of the ground state posses  $C_{2v}$  symmetry. Similarly Si<sub>2</sub>H [\[16](#page-7-10)[,33](#page-7-24)],  $Si<sub>2</sub>Na$  [\[7](#page-7-25)[,10](#page-7-5)], neutral  $Si<sub>2</sub>Li$  have a <sup>2</sup>A<sub>1</sub>ground state with a low-lying  ${}^{2}B_1$  excited state. This latter state is only 0.11 and 0.16 eV higher in energy at the B3LYP and BPW91 levels of theory, respectively. The Li–Si bond lengths are predicted to be 2.615 Å at the B3LYP level of theory, which is in excellent agreement with the values of 2.63 Å predicted by the MP2/6-31G(d) method  $[11]$  $[11]$ .

The Si<sub>2</sub>Li<sup>-</sup> anion displays  $C_{2v}$  symmetry with <sup>1</sup>A<sub>1</sub> state. As we can observe from Fig. [1,](#page-1-0) the Li–Si bond lengths of anion are shorter than that of the neutral by 0.10 Å at the B3LYP level of theory. The reason (based on the reported  $Si<sub>n</sub>Na$  system described by Kishi et al. [\[8](#page-7-3)]) is that the additional electron going into the SOMO of the neutral Si*n*Li becomes doubly occupied in the anion, which localizes



<span id="page-1-0"></span>**Fig. 1** The optimized geometries for neutral  $Si<sub>2</sub>Li$  and the corresponding anion in which only silicon atoms are numbered. In the figure the B3LYP bond lengths (in Å) are shown whereas the remaining DFT parameters have been displayed in the supporting information of this article



<span id="page-2-0"></span>Fig. 2 The optimized geometries for neutral Si<sub>3</sub>Li and the corresponding anion in which only silicon atoms are numbered. In the figure the B3LYP bond lengths (in  $\AA$ ) are shown whereas the remaining DFT parameters have been displayed in the supporting information of this article



<span id="page-2-1"></span>Fig. 3 The optimized geometries for neutral Si<sub>4</sub>Li and the corresponding anion in which only silicon atoms are numbered. In the figure the B3LYP bond lengths (in Å) are shown whereas the remaining DFT parameters have been displayed in the supporting information of this article



<span id="page-2-2"></span>**Fig. 4** The optimized geometries for neutral  $Si<sub>5</sub>Li$  and the corresponding anion in which only silicon atoms are numbered. In the figure the B3LYP Li–Si bond lengths (in Å) are shown whereas the remaining DFT parameters have been displayed in the supporting information of this article

mainly on the  $Si_n$  framework. However, the electron back-donation from the  $Si<sub>n</sub>$  framework to the Li atom is induced and makes the bond between the Si*n* and Li atoms strong.

The theoretical neutral-anion energies for  $Si<sub>n</sub>Li$  (*n* = 2–10) are listed in Table [1.](#page-3-2) The  $EA_{ad}$ ,  $EA_{vert}$ , and VDE for Si2Li are, respectively, predicted to be 1.74, 1.69, and 1.79 eV at the BPW91 level of theory, which resemble the B3LYP values. The B3LYP values are slightly larger than the



<span id="page-2-3"></span>**Fig. 5** The optimized geometries for neutral  $Si<sub>6</sub>Li$  and the corresponding anion in which only silicon atoms are numbered. In the figure the B3LYP Li–Si bond lengths (in Å) are shown whereas the remaining DFT parameters have been displayed in the supporting information of this article



<span id="page-2-4"></span>**Fig. 6** The optimized geometries for neutral  $Si<sub>7</sub>Li$  and the corresponding anion in which only silicon atoms are numbered. In the figure the B3LYP Li–Si bond lengths (in Å) are shown whereas the remaining DFT parameters have been displayed in the supporting information of this article



<span id="page-2-5"></span>**Fig. 7** The optimized geometries for neutral  $Si_8Li$  and the corresponding anion in which only silicon atoms are numbered. In the figure the B3LYP Li–Si bond lengths (in Å) are shown whereas the remaining DFT parameters have been displayed in the supporting information of this article

BPW91 values by 0.05 eV. No experimental data are available for comparison.

3.2 Si<sub>3</sub>Li and Si<sub>3</sub>Li<sup>-</sup>

The geometries of the ground state  $Si<sub>3</sub>Li$  and its anion are displayed in Fig. [2.](#page-2-0) Previous studies have indicated that the geometries of the ground state of  $Si<sub>3</sub>Li$  have  $C<sub>2v</sub>$  symmetry  $[11, 12, 14]$  $[11, 12, 14]$  $[11, 12, 14]$  $[11, 12, 14]$  $[11, 12, 14]$ . Similarly Si<sub>3</sub>H  $[34, 35]$  $[34, 35]$  and Si<sub>3</sub>Na [\[7](#page-7-25)], the neutral



<span id="page-3-0"></span>Fig. 8 The optimized geometries for neutral  $Si_8Li$  and the corresponding anion in which only silicon atoms are numbered. In the figure the B3LYP Li–Si bond lengths (in  $\AA$ ) are shown whereas the remaining DFT parameters have been displayed in the supporting information of this article



<span id="page-3-1"></span>**Fig. 9** The optimized geometries for neutral  $Si<sub>10</sub>Li$  and the corresponding anion in which only silicon atoms are numbered. In the figure the B3LYP Li–Si bond lengths (in Å) are shown whereas the remained of the DFT parameters have been displayed in the supporting information of this article

Si<sub>3</sub>Li has a <sup>2</sup>A<sub>1</sub> ground state with a low-lying <sup>2</sup>B<sub>2</sub> excited state. Again, the latter state is only higher in energy by 0.15 and 0.14 eV at the B3LYP and BPW91 levels of theory, respectively. The Li–Si bond lengths are calculated to be 2.541 Å at the B3LYP level of theory, which are in agreement with the values of 2.55 Å predicted at the MP2/6-31G(d) level of theory [\[11](#page-7-6)]. For the negatively charged ion Si3Li−, the ground state structure has  $C_{2v}$  symmetry with <sup>1</sup>A<sub>1</sub> state. The Li–Si bond lengths of anion Si3Li<sup>−</sup> are shorter than that of neutral by 0.08 Å at the B3LYP level. The reason is described earlier.

For Si3Li, the EAad, EAvert, and VDE are 1.98, 1.96, and 2.04 eV at the BPW91 level of theory, respectively. As can be seen from Table [1,](#page-3-2) the B3LYP values are in good agreement with the BPW91 values, but again lack of experimental data prevents us from making a methodological recommendation.

#### 3.3 Si4Li and Si4Li<sup>−</sup>

The geometries of the ground state structures  $Si<sub>4</sub>Li$  and its anions are displayed in Fig. [3.](#page-2-1) The ground state structure for Si<sub>4</sub>Li is  $C_s$  symmetry with <sup>2</sup>A'' state which is in agreement

<span id="page-3-2"></span>**Table 1** The zero-point corrected adiabatic electron affinity  $(EA_{ad})$ , the vertical electron affinity (EAvert), and the vertical detachment energy (VDE) for the  $Si<sub>n</sub>Li$  ( $n = 2-10$ ) clusters, all of which are in units of eV

<b>Species</b>	Method	$EA_{ad}$	EA <sub>vert</sub>	<b>VDE</b>
$Si2Li(^{2}A1 \leftarrow1 A1)$	B3LYP	1.79	1.74	1.83
	BPW91	1.74	1.69	1.79
$Si3Li(^{2}A1 \leftarrow^{1}A1)$	B3LYP	1.97	1.94	2.03
	BPW91	1.98	1.96	2.04
$Si_4Li(^2A'' \leftarrow^1 A_1)$	B3LYP	1.78	1.18	2.41
	BPW91	1.84	1.25	2.39
$Si5Li(^{2}A' \leftarrow^{1} A')$	B3LYP	2.46	2.05	2.85
	BPW91	2.45	2.03	2.83
$Si_6Li(^2A' \leftarrow^1 A')$	B3LYP	2.24	2.14	2.37
	BPW91	2.24	2.15	2.36
$Si7Li2B2 \leftarrow1C1$	B3LYP	2.23	1.46	2.71
	BPW91	2.23	1.42	2.75
$Si_8Li(^2B_2 \leftarrow^1 A_1)$	B3LYP	2.98	2.72	3.22
	BPW91	2.98	2.76	3.19
$\text{Si}_9\text{Li}({}^1C_1 \leftarrow {}^1A')$	B3LYP	2.90	2.27	3.21
	BPW91	3.01	2.27	3.20
$Si10Li2A' \leftarrow$ <sup>1</sup> A')	B3LYP	2.82	2.24	3.40
	BPW91	2.73	2.19	3.33

with previous theoretical studies  $[11, 12, 14]$  $[11, 12, 14]$ . The groundstate structure of  $Si<sub>4</sub>Li$  is different from that of  $Si<sub>4</sub>Na$ , which has  $C_{2v}$  symmetry with <sup>2</sup>B<sub>2</sub> state. It is also different from  $Si<sub>4</sub>H$  [\[7](#page-7-25)[,10](#page-7-5)]. In fact, the H–Si bonds for ground state structures of  $Si<sub>n</sub>H$  with the exception of  $Si<sub>2</sub>H$  and  $Si<sub>3</sub>H$  are stretched bonds. However, the R–Si bonds for ground state geometries of  $Si<sub>n</sub>R$  are bridged. The Li–Si bond lengths of Si4Li are predicted to be 2.506 and 2.597 Å at the B3LYP level of theory, that is in agreement with values of 2.50 and 2.60 Å predicted by the MP2/6-31G(d) theory method [\[11](#page-7-6)]. For the negatively charged ion Si4Li−, the ground state structure has  $C_{2v}$  symmetry with <sup>1</sup>A<sub>1</sub> state. Therefore, the most stable isomer of Si4Li<sup>−</sup> differs from that of neutral Si4Li. The Li–Si bond lengths of Si4Li<sup>−</sup> are predicted to be 2.445 Å at the B3LYP level of theory.

The theoretical  $EA_{ad}$ ,  $EA_{vert}$ , and VDE for  $Si<sub>4</sub>Li$  are predicted to be  $1.84$ ,  $1.25$ , and  $2.39 \text{ eV}$  at the BPW91 level of theory, and 1.78, 1.18, and 2.39 eV at the B3LYP level of theory, respectively. The B3LYP values are close to the BPW91 values. The values of  $EA_{ad}$ ,  $EA_{vert}$ , and VDE are different from each other on account of the large change in geometry between the neutral cluster and its anion.

3.4 Si<sub>5</sub>Li and Si<sub>5</sub>Li<sup>−</sup>

The geometries of ground state  $Si<sub>5</sub>Li$  and its anion are dis-played in Fig. [4.](#page-2-2) For the neutral Si<sub>5</sub>Li cluster, Sporea et al. [\[12](#page-7-7),[14\]](#page-7-8) reported that the geometries of the ground state displayed  $C_s$  symmetry at the B3LYP/6-31+G(d) level of theory. Wang et al. [\[11\]](#page-7-6) reported that it was  $C_{2v}$  symmetry with the MP2/6-31G(d) method. Our DFT computations reveal that this structure has the  $C_{2v}$  symmetry with <sup>2</sup>B<sub>2</sub> state at the BPW91 level of theory. At the B3LYP level of theory, there is an imaginary frequency with a  $b_2$  mode to be found for the  $C_{2v}$  symmetry structure. Following the  $b_2$ mode, the  $C_{2v}$  symmetry collapses to  $C_s$  symmetry with <sup>2</sup>A' state. The  $C_{2v}$  and the  $C_s$  geometry have essentially the same energies The  $C_{2v}$  structure is only higher in energy than the  $C_s$  structure by 0.00009 eV (0.002 kcal/mol). On the other hand, the small imaginary frequencies of  $12 \text{ cm}^{-1}$  for the  $C_{2v}$  structure are thought to be an artifact of the numerical integration. Hence, we assign the  $C_{2v}$  symmetry for the ground state geometry of Si<sub>5</sub>Li at the B3LYP level of theory which is identical to the MP2 result. The Li–Si bond lengths of  $Si<sub>5</sub>Li$  are predicted to be 2.553 Å at the B3LYP level of theory, which are in agreement with values of 2.52 Å predicted by MP2/6-31 $G(d)$ [\[11](#page-7-6)].

For the negatively charged Si<sub>5</sub>Li<sup>−</sup> ion, the ground state structure has  $C_s$  symmetry in the <sup>1</sup>A' state. The Li–Si bond lengths of  $Si<sub>5</sub>Li<sup>-</sup>$  are predicted to be 2.509 and 2.723 Å at the B3LYP level of theory, respectively. The theoretical  $EA_{ad}$ ,  $EA_{vert}$ , and VDE for Si<sub>5</sub>Li are predicted to be 2.45, 2.03, and 2.83 eV at the BPW91 level of theory, respectively. As can be seen from Table [1,](#page-3-2) the B3LYP values are in good agreement with the BPW91 values. The values of EAad, EAvert, and VDE are different from each other because of the large change in geometry between neutral cluster and its anion.

### 3.5 Si<sub>6</sub>Li and Si<sub>6</sub>Li<sup>-</sup>

The  $C_{2v}$ -symmetry structure of the <sup>2</sup>B<sub>2</sub> ground state for neutral Si<sub>6</sub>Li and the  $C_{2v}$ -symmetry structure of the <sup>1</sup>A<sub>1</sub> ground state for anion  $Si<sub>6</sub>Li<sup>-</sup>$  are displayed in Fig. [5.](#page-2-3) For neutral  $Si<sub>6</sub>Li$ , our DFT results agree with earlier theoretical studies [\[11](#page-7-6),[12,](#page-7-7)[14\]](#page-7-8). The two equivalent Li–Si bond lengths are predicted to be 2.656 Å and another two equivalent Li–Si bond lengths are predicted to be 2.678 Å at the B3LYP level of theory, which are in agreement with values of 2.62 and 2.68 Å predicted by MP2/6-31G(d), respectively [\[11\]](#page-7-6). These Li– Si bond lengths in anion are shortened from neutral structure by 0.06 and 0.13 Å, respectively.

Our DFT results for  $Si<sub>6</sub>Li<sup>-</sup>$  are different from the earlier studies reported by Li et al. [\[15](#page-7-9)] They asserted that  $Si<sub>6</sub>A^-$  (A = Li, Na, and K) clusters displayed  $C_{3v}$  symmetry (see  $[15]$  $[15]$  for the  $C_{3v}$  symmetry structure). Energetically, the  $C_{3v}$ -symmetry isomer for Si<sub>6</sub>Li<sup>-</sup> is less stable than the  $C_{2v}$ -symmetry by 0.47 and  $0.63 \text{ eV}$  at the B3LYP and the BPW91 levels of theory, respectively. Further computations on  $Si_6K^-$  at the MP2(full)/6-311+G(d) and B3LYP/6 $311+G(d)$  levels of theory reveal that the  $C_{3v}$  symmetry isomers are local minima on the potential energy surface of  $Si<sub>6</sub>K<sup>-</sup>$ . The  $C<sub>2v</sub>$  symmetry structures for  $Si<sub>6</sub>K<sup>-</sup>$  are more stable in energy than the  $C_{3v}$  symmetry by 0.20 and 0.07 eV at MP2(full)/6-311+G(d) and B3LYP/6-311+G(d) levels of theory, respectively. For  $Si<sub>6</sub>Na<sup>-</sup>$ , the ground state structure is also  $C_{2v}$  symmetry [\[8](#page-7-3)[–10,](#page-7-5)[15\]](#page-7-9). That is, the  $C_{3v}$  symmetry isomers are local minima points on the potential energy surface of  $Si<sub>6</sub>A<sup>-</sup>$ . As can be seen from Table [1,](#page-3-2) both the BPW91 and the B3LYP values of  $EA_{ad}$ ,  $EA_{vert}$ , and VDE for  $Si<sub>6</sub>Li$ are in excellent agreement and predicted to be 2.24, 2.15, and 2.36 eV, respectively.

# 3.6 Si7Li and Si7Li<sup>−</sup>

The  $C_{2v}$ -symmetry structures of the <sup>2</sup>B<sub>1</sub> ground state for neutral  $Si<sub>7</sub>Li$  and the  $C<sub>1</sub>$ -symmetry ground state structures for the Si7Li<sup>−</sup> anion are displayed in Fig. [6.](#page-2-4) For the neutral Si7Li, our DFT results agree with earlier theoretical studies [\[11](#page-7-6)]. The two equivalent Li–Si bond lengths are predicted to be 2.554 Å at the B3LYP level of theory, which are in agreement with values of 2.56 Å predicted by MP2/6-31G(d) [\[11](#page-7-6)].

For Si7Li−, the ground state geometries are *distorted rhombohedron* with  $C_1$  symmetry. This result is different from the previous study reported by Li et al. [\[15](#page-7-9)]. They presented that  $Si<sub>7</sub>A^-$  (A = Li, Na, and K) clusters had  $C_s$ symmetry (see  $[15]$  $[15]$  for the  $C_s$  symmetry structure). Energetically, the  $C_s$ -symmetry isomer for  $Si<sub>7</sub>Li<sup>-</sup>$  is less stable than the  $C_1$ -symmetry by 0.35 and  $0.40 \text{ eV}$  at the B3LYP and the BPW91 levels of theory, respectively. Again, further computation on  $Si_7K^-$  with the MP2(full)/6-311+G(d) and B3LYP/6-311+G(d) schemes show that they are  $C_1$  symmetry structures. This species is more stable in energy than the  $C_s$  symmetry by 0.22 and 0.04 eV at MP2(full)/6-311+G(d) and B3LYP/6-311+G(d) levels of theory, respectively. For Si7Na−, the ground state structure is also *distorted rhombohedron* with  $C_1$  symmetry [\[10](#page-7-5)]. That is, the  $C_s$  symmetry isomers are local minima points on the potential energy surface of Si<sub>7</sub>A<sup>-</sup>.

As can be seen from Table [1,](#page-3-2) both the BPW91 and the B3LYP values of  $EA_{ad}$ ,  $EA_{vert}$ , and VDE for  $Si<sub>7</sub>Li$  are in excellent agreement. The theoretical  $EA_{ad}$ ,  $EA_{vert}$ , and  $VDE$ are predicted to be 2.23, 1.42, and 2.75 eV (BPW91 values), respectively. The values of EAad, EAvert, and VDE are, again, different from each other due to the large changes in geometry between the neutral cluster and its anion.

## 3.7 Si<sub>8</sub>Li and Si<sub>8</sub>Li<sup> $-$ </sup>

The  $C_s$ -symmetry structure of the <sup>2</sup>A" ground state for neutral Si<sub>8</sub>Li and the  $C_{2v}$ -symmetry structure of the <sup>1</sup>A<sub>1</sub> ground state for anion  $Si_8Li^-$  are displayed in Fig. [7.](#page-2-5) For the  $Si_8Li$  neutral structure, the two equivalent Li–Si, Li–2Si, and Li–2Si bond lengths are predicted to be 2.636, 2.691, and 2.710 Å at the B3LYP level of theory, respectively.

For Si8Li−, the Li–Si bond lengths are shorter than corresponding bonds in neutral by 0.10 Å. One can note that the DFT results are different from the previous study reported by Li et al. [\[15\]](#page-7-9). They presented that the  $Si<sub>8</sub>A^-$  clusters had  $C_1$  symmetry. In fact, the  $C_1$  structures for  $Si_8K^-$  are less stable in energy than the  $C_{2v}$  symmetry by 0.63 and 0.91 eV at MP2(full)/6-311+G(d) and B3LYP/6-311+G(d) levels of theory, respectively. That is, the ground state geometries for  $Si<sub>8</sub>A^-$  display  $C_{2v}$  symmetry with <sup>1</sup>A<sub>1</sub> state (for Si<sub>8</sub>Na<sup>-</sup>, see  $[10]$  $[10]$ ). The  $C_1$  symmetry isomers are local minima points on the potential energy surface of  $Si<sub>8</sub>A<sup>-</sup>$ .

As can be seen from Table [1,](#page-3-2) both the BPW91 and the B3LYP values of  $EA_{ad}$ ,  $EA_{vert}$ , and VDE for  $Si_8Li$  are, again, in excellent agreement. The theoretical  $EA_{ad}$ ,  $EA_{vert}$ , and VDE are predicted to be 2.98, 2.76, and 3.19 eV (BPW91 values), respectively.

## 3.8 Si9Li and Si9Li<sup>-</sup>

The *C*<sub>1</sub>-symmetry ground state structure for neutral Si<sub>9</sub>Li and  $C_s$ -symmetry structure of the  ${}^{1}A'$  ground state for anion Si9Li<sup>−</sup> are displayed in Fig. [8.](#page-3-0) For Si9Li, the three Li–Si bond lengths are predicted to be 2.626, 2.723, and 2.619 Å at the B3LYP level of theory, respectively. For Si9Li−, the two equivalent Li–6Si and Li–7Si bond distances are predicted to be 2.711 Å, the two equivalent Li–4Si and Li–5Si bond distances are predicted to be 2.604 Å, and the Li–1Si bond lengths are predicted to be 2.531 Å at the B3LYP level of theory. The ground state structures of Si9Li<sup>−</sup> differ from those of Si<sub>9</sub>K<sup> $-$ </sup> that have  $C_{3v}$  symmetry structures [\[15](#page-7-9)[,20](#page-7-12)]. The theoretical  $EA_{ad}$  for Si<sub>9</sub>Li are predicted to be 2.90 and 3.01 eV at the B3LYP and the BPW91 levels of theory, respectively. The EAvert and VDE are predicted to be 2.27 and 3.20 eV at both the B3LYP and the BPW91 levels of theory, respectively.

3.9 Si<sub>10</sub>Li and Si<sub>10</sub>Li<sup>-</sup>

The  $C_s$ -symmetry structure of the <sup>2</sup>A' ground state for  $Si_{10}Li$ and  $C_s$ -symmetry structure of the  ${}^{1}A'$  ground state for  $Si<sub>10</sub>Li<sup>-</sup>$  are displayed in Fig. [9.](#page-3-1) For neutral  $Si<sub>10</sub>Li$ , the two equivalent Li–5Si and Li–6Si bond lengths are predicted to be 2.631 Å and the Li–8Si bond distances are predicted to be 2.606 eV at the B3LYP level of theory. It is useful to mention that Majumder  $[36]$  $[36]$  studied the impurity-doped  $Si<sub>10</sub>$ cluster and Sporea and Rabilloud [\[37\]](#page-7-29) reported stability of alkali-encapsulating silicon cage clusters. For  $Si<sub>10</sub>Li<sup>-</sup>$ , the two equivalent Li–5Si and Li–9Si bond lengths are predicted to be 2.609 Å, and the Li–6Si bond distances are predicted to be 2.557 eV at the B3LYP level of theory.

The theoretical EA<sub>ad</sub>, EA<sub>vert</sub>, and VDE for  $Si<sub>10</sub>Li$  are predicted to be 2.73, 2.19, and 3.33 eV at the BPW91 level of theory, respectively. The B3LYP values are slightly larger than those of the BPW91 by 0.07 eV seen in Table [1.](#page-3-2) The values of EA<sub>ad</sub>, EA<sub>vert</sub>, and VDE are, again, different from each other due to the large change in geometry between neutral cluster and its anion seen in Fig. [9.](#page-3-1)

It is interesting to note that the ground state structure for neutral  $Si<sub>n</sub>Li$  keeps the  $Si<sub>n</sub>$  framework unchanged [\[11](#page-7-6)[,12](#page-7-7)]. For Si*n*Li−, the ground state structure also keeps the corresponding  $\text{Si}_n$  (or  $\text{Si}_n^-$ ) framework unchanged when  $n \leq 6$ , while the corresponding  $\mathrm{Si}_n$  (or  $\mathrm{Si}_n^-$ ) framework changes largely when  $n \ge 7$ . For electron affinities, the values predicted by the B3LYP and the BPW91 are very close. This result may indicate that the electron affinity predicted by these methods is right and close to experimental value because actual electron affinity is the one and only.

#### 3.10 Dissociation energies

The dissociation energy  $(D_e)$  (defined as the energy required in the reaction  $Si_nLi \rightarrow Si_n+Li$  for  $Si_nLi$  species are evaluated and exhibited in Table [2.](#page-6-0) Rabilloud and coworkers [\[12\]](#page-7-7) calculated the  $D_e$  for  $Si<sub>n</sub>Li$  with *n* from 1 to 6. As can be seen from Table [2,](#page-6-0) the energy difference between the B3LYP and the BPW91 values is within 0.10 eV. In Fig. [10,](#page-6-1) the BPW91  $D_e$  for  $Si_nLi$  and  $Si_nNa$  (see [\[10\]](#page-7-5)) as a function of the size of the clusters is shown. As can be seen from Fig. [10,](#page-6-1) the two parallel oscillating curves, the top curve for Si*n*Li and the lower curve for  $Si<sub>n</sub>Na$ , show that (i) the dissociation energies are local minima for  $n = 4$  and 7, and local maxima for  $n = 2$ , 5, and 8. In other words,  $Si<sub>n</sub>Li$  and  $Si<sub>n</sub>Na$  for  $n = 4$ and 7 are less stable than when  $n = 2$ , 5 and 8. These also indicate that  $Si_n$  for  $n = 4$  and 7 are more stable and for  $n = 2, 5$ , and 8 are less stable. This result is consistent with previous results with respect to Si*n* [\[20](#page-7-12),[38,](#page-7-30)[39\]](#page-7-31) (ii) as expected the dissociation energies of lithium atom are larger than that of sodium. That is, Li adsorption on surface of silicon clusters is more stable than Na. This result is in agreement with experimental observations [\[17](#page-7-32)]. The reason is that the small size of Li atoms results in a higher stability.

The  $D_e$  (defined as the energy required in the reaction Si*n*Li<sup>−</sup> → Si<sup>−</sup> *<sup>n</sup>* +Li) of Si*n*Li<sup>−</sup> cluster is also calculated and is displayed in Table [3.](#page-6-2) The BPW91 D*e* for the Si*n*Li− and  $Si<sub>n</sub>Na<sup>-</sup>$  (see [\[10](#page-7-5)]) as a function of the size of the clusters is also shown in Fig. [11.](#page-6-3) The energies difference between the B3LYP and the BPW91 values are within 0.08 eV seen in Table [3.](#page-6-2) The top curve in Fig. [11](#page-6-3) shows that the *D*e of  $Si<sub>n</sub>Li<sup>-</sup>$  is local minima for *n* = 4 and 7 and local maxima for  $n = 2, 5$ , and 9. That is, Si<sub>4</sub>Li<sup>-</sup> and Si<sub>7</sub>Li<sup>-</sup> are less stable and Si<sub>2</sub>Li<sup>-</sup>, Si<sub>5</sub>Li<sup>-</sup>, and Si<sub>9</sub>Li<sup>-</sup> are more stable. The two curves in Fig. [11](#page-6-3) also show that the dissociation energies

<span id="page-6-0"></span>**Table 2** Dissociation energies  $(D_e)$  for the Neutral  $Si_nLi$  ( $n = 2-10$ ) clusters in eV. The values displayed in *parenthesis* correspond to zeropoint vibrational energies. It is also useful to note that the B3LYP and the BPW91 calculations on the ground state structures of  $Si<sub>n</sub>$  have been presented in [\[20\]](#page-7-12)

Dissociation	B3LYP	BPW91
$Si2Li \rightarrow Si2+Li$	2.33(2.29)	2.43(2.39)
$Si3Li \rightarrow Si3+Li$	2.20(2.16)	2.19(2.15)
$Si_4Li \rightarrow Si_4+Li$	1.63(1.60)	1.73(1.70)
$Si5Li \rightarrow Si5+Li$	2.16(2.12)	2.25(2.12)
$Si_6Li \rightarrow Si_6+Li$	1.89(1.85)	2.00(1.95)
$Si7Li \rightarrow Si7+Li$	1.45(1.41)	1.39(1.37)
$Si_8Li \rightarrow Si_8+Li$	2.17(2.11)	2.19(2.14)
$Si9Li \rightarrow Si9+Li$	1.78(1.72)	1.70(1.65)
$Si10Li \rightarrow Si10+Li$	1.67(1.64)	1.66(1.63)



<span id="page-6-1"></span>**Fig. 10** Dissociation energies (computed using uncorrected zero-point vibrational energies) of  $\text{Si}_n \text{R} (\text{Si}_n \text{R} \rightarrow \text{Si}_n + \text{R})$  (where  $\text{R} = \text{Li}$ , Na and as for  $Si<sub>n</sub>Na$ , see [\[10](#page-7-5)]) calculated using the BPW91 method and plotted versus the number of atoms *n* in the clusters

of lithium atom are larger than that of sodium. The reason is described above.

# **4 Conclusions**

The present work has provided a systematic study of the Si*n*Li/Si*n*Li− clusters with two carefully selected DFT methods. The lowest energy structures of these clusters have been reported, and we have focused on the neutral Si*n*Li clusters with *n* from 8 to 10 and anions  $Si<sub>n</sub>Li<sup>-</sup>$  with *n* up to 10. The predicted ground state structure is believable when compared with MP2 level of theory. The ground state structures of the neutral Si*n*Li clusters keep the corresponding Si*n* framework. For Si*n*Li−, the lowest energy structures also keep

<span id="page-6-2"></span>**Table 3** Dissociation energies ( $D_e$ ) for the Si<sub>n</sub>Li<sup>-</sup> ( $n = 2-10$ ) anions in units of eV. The values displayed in parenthesis correspond to zeropoint vibrational energies. As in the previous table, the B3LYP and the BPW91 computed results for the ground state structures of  $Si<sub>n</sub>$  have been presented in [\[20\]](#page-7-12)

Dissociation	B3LYP	BPW91
$Si2Li- \rightarrow Si2-+Li$	2.06(2.02)	2.01(1.98)
$Si_3Li^- \rightarrow Si_3^-+Li$	1.85(1.79)	1.87(1.81)
$Si_4Li^- \rightarrow Si4- + Li$	1.27(1.22)	1.33(1.29)
$Si_5Li^- \rightarrow Si_5^- + Li$	2.15(2.10)	2.19(2.15)
$Si_6Li^-\rightarrow Si_6^-+Li$	2.01(1.95)	2.14(2.08)
$Si7Li- \rightarrow Si7- + Li$	1.58(1.53)	1.58(1.53)
$Si_8Li^- \rightarrow Si_8^- + Li$	2.28(2.20)	2.35(2.27)
$Si_9Li^- \rightarrow Si_9^- + Li$	2.37(2.31)	2.45(2.39)
$Si_{10}Li^{-} \rightarrow Si_{10}^{-} + Li$	2.02(1.98)	1.94(1.90)



<span id="page-6-3"></span>**Fig. 11** Dissociation energies (uncorrected with zero-point vibrational energies) of  $\text{Si}_n \text{R}$  ( $\text{Si}_n \text{R}^ \rightarrow$   $\text{Si}_n^- + \text{R}$ ) (where R = Li, Na and as for Si<sub>n</sub>Na<sup>−</sup>, see [\[10\]](#page-7-5)) calculated using the BPW91 method and plotted versus the number of atoms *n* in the clusters

the corresponding  $\mathrm{Si}_n$  (or  $\mathrm{Si}_n^-$ ) framework unchanged when  $n \leq 6$ , while the corresponding  $Si_n$  framework is modified when  $n \geq 7$ . The ground state structures of  $Si_nK^{-}(n = 6)$ , 7, and 8) have been modified when compared with Si*n*Li−. The adiabatic electron affinity, the vertical electron affinity, and the vertical detachment energy for Si*n*Li have been estimated. The values predicted by the B3LYP and the BPW91 schemes are very close. The dissociation energies of Li from the lowest energy structures of  $Si_nLi/Si_nLi^-$  ( $n = 2-10$ ) have been calculated and used to understand relative stability. To the best of our knowledge, there are no experimental data regarding the adiabatic electron affinity and dissociation for these systems. Our results may thus provide a reference for further investigations.

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